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# Spectroscopic properties of Er<sup>3+</sup>/Yb<sup>3+</sup> co-doped 50SiO<sub>2</sub>-20Al<sub>2</sub>O<sub>3</sub>-30CaF<sub>2</sub> glass and glass ceramics

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## Abstract

A spectroscopic investigation of  $Er^{3+}/Yb^{3+}$  co-doped  $50SiO_2-20Al_2O_3-30CaF_2$  glasses and transparent glass ceramics containing  $CaF_2$  nanocrystals is presented. The formation of  $CaF_2$  nanocrystals in the glass ceramic was confirmed by x-ray diffraction (XRD) and transmission electron microscopy (TEM). The Judd–Ofelt parameters of the  $Er^{3+}$  ions in the glass and glass ceramic have been calculated; they suggested that  $Er^{3+}$  ions had been incorporated into  $CaF_2$  nanocrystals in the glass ceramic was much stronger than that of the  $Er^{3+}/Yb^{3+}$  co-doped glass. The upconversion luminescence mechanism has been ascribed to a two-photon absorption process for the green and red luminescence and a three-photon absorption process for the blue luminescence.

# 1. Introduction

 $\rm Er^{3+}$ -doped glasses have attracted great attention because of their potential applications in optoelectronic fields, such as glass lasers, optoelectronic communication devices, sensors and color displays [1–6]. Co-doping with Yb<sup>3+</sup> can greatly enhance the luminescence intensity of  $\rm Er^{3+}$  ions owing to the efficient energy transfer from the Yb<sup>3+</sup>:<sup>2</sup>F<sub>5/2</sub> to the  $\rm Er^{3+}$ :<sup>4</sup>I<sub>11/2</sub> state, because both Yb<sup>3+</sup> and  $\rm Er^{3+}$  ions have an absorption band around 980 nm and the absorption cross section of Yb<sup>3+</sup> ions is much larger than that of  $\rm Er^{3+}$  ions [7–9]. So far, researchers' efforts have already realized the commercialization of  $\rm Er^{3+}/Yb^{3+}$  co-doped glass fibres and optical amplifiers. However, almost all these applied glasses are fluoride glasses, which have

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some disadvantages in chemical and mechanical stabilities. Oxyfluoride glass ceramics doped with rare earth ions have been investigated widely in the past, since they possess not only higher chemical and mechanical stability than fluoride glass but also lower phonon energy than oxide glass [10]. Those glass ceramics usually contain such small crystalline phases as the nanosize  $Pb_xCd_{1-x}F_2$  or  $PbF_2$  crystals in the glass hosts that they can improve the optical properties with no loss of the transparency [11]. However, both  $CdF_2$  and  $PbF_2$  are toxic raw materials.  $CaF_2$  is selected instead of  $CdF_2$  and  $PbF_2$  as one of the raw materials in the present study. CaF<sub>2</sub> is an important optical raw material with high solubility of both sensitizer and activator rare earth ions [12]. Recently, more interest has been focused on rare earth ion doped CaF2 due to potential applications in optoelectronic devices. Extensive studies have been carried out on the optical properties of rare earth ion doped  $CaF_2$  single crystals [13–17]. The same material as thin films deposited on Si substrates has also been studied [18, 19].  $CaF_2:Er^{3+}$  optical waveguides grown by molecular beam epitaxy have recently been demonstrated [20-22]. Furthermore, crystalline CaF<sub>2</sub> is highly transparent from 0.13 to 9.5  $\mu$ m and gives a better matching of refractive index with the aluminosilicate glassy host. This leads to possibilities of preparing transparent glass ceramics containing  $CaF_2$  nanocrystals. This paper presents a detailed spectroscopic investigation of  $Er^{3+}/Yb^{3+}$ co-doped 50SiO<sub>2</sub>-20Al<sub>2</sub>O<sub>3</sub>-30CaF<sub>2</sub> glass and transparent glass ceramics containing CaF<sub>2</sub> nanocrystals. The formation of  $CaF_2$  nanocrystals in the  $50SiO_2-20Al_2O_3-30CaF_2$  glass is confirmed by XRD and TEM. The difference in oscillator strengths between glass and glass ceramics is discussed on the basis of a Judd-Ofelt intensity analysis. The upconversion luminescence and near-infrared luminescence of Er<sup>3+</sup>/Yb<sup>3+</sup> co-doped glasses and glass ceramics are described.

## 2. Experimental details

The 5 mol% YbF<sub>3</sub> and 0.5 mol% ErF<sub>3</sub> co-doped  $50SiO_2-20Al_2O_3-30CaF_2$  oxyfluoride glasses were prepared from high purity SiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub>, CaF<sub>2</sub>, YbF<sub>3</sub> and ErF<sub>3</sub> raw materials. The batches of the raw materials were melted at 1400 °C for 45 min in a covered corundum crucible in normal atmosphere. The melt was poured on a brass mould and then pressed by another brass plate. The glass samples (named as GErYb) were finally obtained. The glass ceramic samples (named as GCErYb) were prepared by heat treatment of the glasses for 2 h at 660 °C, chosen based on DTA measurements. In addition, the 0.5 mol% ErF<sub>3</sub> doped  $50SiO_2-20Al_2O_3-30CaF_2$ oxyfluoride glasses (named as GEr) were also prepared in the same molten conditions. Then the glass and glass ceramic samples were polished on a UNIPOL-802 precision lapping/polishing machine. Glass and glass ceramic samples transparent in visible light were finally obtained.

DTA measurements were carried out in a CDR-1 differential thermal analyser in normal atmosphere in order to confirm the glass transition temperature  $(T_g)$  and crystallization peak temperature  $(T_x)$ . X-ray diffraction measurements were performed with a XD-98 diffractometer with Cu K $\alpha$  radiation at 4° min<sup>-1</sup> scanning rate. TEM images were taken with a JEM4000 FX microscope (JEOL) and the TEM samples were prepared by mechanical polishing and subsequent ion-milling. Densities were measured using the Archimedes principle, with distilled water as the medium. Refractive indices were measured on a Metricom-2010 prism coupler at 632.8, 1300 and 1549 nm. Optical absorption measurements were performed on a Hitachi UV-4100 spectrophotometer. For luminescence spectra measurements: (1) direct luminescence spectra were measured with a slit resolution of 2.5 nm on a Hitachi F-4500 fluorescence spectrophotometer by excitation of a Xe lamp; (2) upconversion luminescence spectra were measured with a slit resolution of 1.0 nm on a Hitachi F-4500 fluorescence spectrophotometer using 980 nm excitation from a laser diode; (3) 980 nm (laser) excited near-

infrared luminescence and 1064 nm (laser) excited decay spectra were measured with a Horiba Triax-550 monochromator. All measurements were performed at room temperature.

### 3. Theoretical details

From the absorption spectrum, the oscillator strengths of the electronic transitions can be calculated using the expression

$$P_{\exp} = \frac{2303mc^2}{\pi e^2 N_0} \int \varepsilon(\nu) \,\mathrm{d}\nu \tag{1}$$

where *m* is the electron mass (g) and *e* is the electron charge (electrostatic units), *c* is the velocity of light,  $N_0$  is the Avogadro constant, and  $\varepsilon(\nu)$  is the molar extinction coefficient at the wavenumber  $\nu$  (cm<sup>-1</sup>), which can be computed from the Beer–Lambert law:

$$\varepsilon(\nu) = \frac{\log(I_0/I)}{Cd} \tag{2}$$

where  $\log(I_0/I)$  is the measured absorbance at the wavenumber  $\nu$  (cm<sup>-1</sup>), *C* is the concentration of the lanthanide ions (mol/1000 cm<sup>3</sup>) and *d* is the light path in the measured sample (cm) [23, 24].

According to the Judd–Ofelt theory [25, 26], the oscillator strength of the  $aJ \rightarrow bJ'$  transition (at the wavenumber  $\nu$ ) can be calculated from

$$P_{\rm cal} = P_{\rm ed} + P_{\rm md} = \frac{8\pi^2 m c \nu}{3h(2J+1)e^2n^2} \left(\chi_{\rm ed}S_{\rm ed} + \chi_{\rm md}S_{\rm md}\right)$$
(3)

where  $\chi$  is the term for the effective field at a well-localized centre [27] in a medium of isotropic refractive index *n*, which for electric-dipole transitions and magnetic-dipole transitions, respectively, is given by

$$\chi_{\rm ed} = \frac{n(n^2 + 2)^2}{9} \qquad \text{(for electric-dipole transitions)} \tag{4}$$

$$\chi_{\rm md} = n^3$$
 (for magnetic-dipole transitions). (5)

The electric dipole and magnetic dipole,  $S_{ed}$  and  $S_{md}$ , are expressed as

$$S_{\rm ed}(aJ, bJ') = e^2 \sum_{t=2,4,6} \Omega_t \left| \left\langle aJ \left| U^{(t)} \right| bJ' \right\rangle \right|^2 \tag{6}$$

$$S_{\rm md}(aJ, bJ') = \frac{e^2}{4m^2c^2} \left| \left\langle aJ \left| L + 2S \right| bJ' \right\rangle \right|^2.$$
(7)

However, it must be noted that only the magnetic dipolar transitions, with selection rules  $\Delta S = \Delta L = 0$ ,  $\Delta J = 0$ ,  $\pm 1$ , could contribute efficiently to the oscillator strength of rare earth ions [28].

The  $\Omega_t$  parameters, known as Judd–Ofelt (JO) parameters, can be determined from a leastsquares fit to the values of measured oscillator strengths using equation (3). The reduced matrix elements of  $|\langle aJ|U^{(t)}|bJ'\rangle|^2$  and the expression of  $|\langle aJ|L + 2S|bJ'\rangle|^2$  have been given by some researchers [1, 6]. A measure of the accuracy of the fit is given by the root-mean-square (rms) deviation:

rms = 
$$\left[\frac{\Sigma (P_{cal} - P_{exp})^2}{(\xi - 3)}\right]^{1/2}$$
 (8)

where  $\xi$  is the number of transitions analysed.



Figure 1. DTA curve of the 5 mol%  $YbF_3$  and 0.5 mol%  $ErF_3$  co-doped  $50SiO_2-20Al_2O_3-30CaF_2$  glass.

The spontaneous emission probabilities A(aJ, bJ') of the different electronic transitions are given in the Judd–Ofelt theory by

$$A(aJ, bJ') = A_{\rm ed} + A_{\rm md} = \frac{64\pi^4 \nu^3}{3h(2J+1)} \left(\chi_{\rm ed}S_{\rm ed} + \chi_{\rm md}S_{\rm md}\right).$$
(9)

The emission branching ratio of a transition is defined as

$$\beta(aJ, bJ') = \frac{A(aJ, bJ')}{\sum_{bJ'} A(aJ, bJ')}$$
(10)

and the radiative lifetime of an emitting state is related to the total spontaneous emission probabilities for all transitions from this state by

$$\tau = \frac{1}{\sum_{bJ'} A(aJ, bJ')} \tag{11}$$

where the sum is extended over all the states at energies lower than aJ.

For direct excitation, the luminescence quantum yield,  $\eta$ , is defined as

$$\eta = \frac{\text{emitted light intensity}}{\text{absorbed radiation intensity}} = \frac{\tau_{\text{exp}}}{\tau_{\text{cal}}}$$
(12)

where  $\tau_{exp}$  is the observed lifetime and  $\tau_{cal}$  is the lifetime calculated from equation (11).

# 4. Results and discussion

Figure 1 shows the DTA curve of GErYb where  $T_g$  (590 °C),  $T_{X1}$  (680 °C) and  $T_{X2}$  (840 °C) stand for the glass transition temperature, and the first and the second crystallization temperature, respectively. XRD analysis showed that the first crystallization peak,  $T_{X1}$ , could be ascribed to the precipitation of CaF<sub>2</sub> crystals and the second crystallization peak,  $T_{X2}$ , to the bulk crystallization process of the glass matrix. Thus 660 °C, a little lower than  $T_{X1}$ , was selected as the heat treatment temperature for the precipitation of CaF<sub>2</sub> nanocrystals from the glassy matrix.

Figure 2 shows the XRD patterns of GErYb and GCErYb, respectively. GErYb is completely amorphous with no diffraction peaks. But the intense diffraction peaks were observed for the XRD curve of GCErYb, and these diffraction peaks can be easily assigned



Figure 2. XRD pattern of Er<sup>3+</sup>/Yb<sup>3+</sup> co-doped glass (GErYb) and glass ceramic (GCErYb).



**Figure 3.** TEM image of  $Er^{3+}/Yb^{3+}$  co-doped glass ceramic.

to the  $CaF_2$  cubic phase. From the obtained peak width of XRD pattern, the size of  $CaF_2$  nanocrystals in GCErYb can be calculated by the Sherrer formula:

$$D_{hkl} = \frac{K\alpha}{\beta\cos\theta} \tag{13}$$

where  $D_{hkl}$  is the crystal size normal to (hkl),  $\lambda$  is the x-ray wavelength,  $\theta$  is the angle of diffraction,  $\beta$  is the full-width at half-maximum (FWHM) of the diffraction peak and the constant K = 0.90. The CaF<sub>2</sub> crystal size can be calculated to be about 10 nm. Figure 3 shows a TEM image of the glass ceramic GCErYb. The size of the roughly spherical particles can be found to be approximately 10 nm, which is consistent with the Scherrer-calculated diameter.

Some physical properties of GErYb and GCErYb are presented in table 1. The refractive indices at 632.8, 1300 and 1549 nm were used to determine the relations between the refractive index and the wavelength by a least-squares fitting to the Sellmeier dispersion equation [29]

$$n^2(\lambda) = 1 + \frac{S\lambda^2}{\lambda^2 - \lambda_0^2}.$$
(14)



**Figure 4.** Absorption spectra of GEr, GErYb and GCErYb. The absorption bands were assigned to the transitions from the ground state to the state: (0)  ${}^{4}G_{11/2}$ ; (1)  ${}^{2}H_{9/2}$ ; (2)  ${}^{4}F_{5/2,3/2}$ ; (3)  ${}^{4}F_{7/2}$ ; (4)  ${}^{2}H_{11/2}$ ; (5)  ${}^{4}S_{3/2}$ ; (6)  ${}^{4}F_{9/2}$ ; (7)  ${}^{4}I_{9/2}$ ; (8)  ${}^{4}I_{11/2}$ ; (9)  ${}^{4}I_{13/2}$ .

Table 1. Some physical properties of GErYb and GCErYb.

Sample name	GErYb	GCErYb
Density (g cm <sup>-3</sup> )	3.039	2.923
Thickness (cm)	0.060	0.061
$Er^{3+}$ concentration (mol dm <sup>-3</sup> )	0.171	0.170
Refractive index (at 632.8 nm)	1.507	1.507
Refractive index (at 1300 nm)	1.510	1.510
Refractive index (at 1549 nm)	1.516	1.515

**Table 2.** The calculated refractive indices, *n*, and experimental and calculated oscillator strengths, *P*, of the  $\text{Er}^{3+}$  absorption transitions from the ground state  ${}^{4}\text{I}_{15/2}$  to the [SL]J states (for GErYb: rms =  $1.52 \times 10^{-7}$ ; for GCErYb: rms =  $1.10 \times 10^{-7}$ ).

Excited			GErYb				GCErYb	
state	$\lambda$ (nm)	п	$P_{\rm exp} \times 10^8$	$P_{\rm cal} \times 10^8$	$\lambda$ (nm)	п	$P_{\rm exp} \times 10^8$	$P_{\rm cal} \times 10^8$
<sup>4</sup> I <sub>13/2</sub>	1531	1.533	168.6	166.7	1529	1.523	164.4	113.6
$^{4}I_{11/2}$	_	_	_	_	_	_	_	_
$^{4}I_{9/2}$	796	1.541	23.3	30.5	800	1.530	22.6	26.7
$^{4}F_{9/2}$	651	1.546	209.0	203.4	652	1.535	189.9	186.2
$^{4}S_{3/2}$	541	1.554	67.3	45.0	539	1.542	51.8	44.6
$^{2}H_{11/2}$	521	1.556	823.8	814.2	521	1.544	559.4	557.2
$^{4}F_{7/2}$	488	1.560	167.5	186.7	487	1.547	164.6	179.4
$^{4}F_{5/2,3/2}$	451	1.566	71.2	85.2	449	1.552	75.0	84.3
$^{2}H_{9/2}$	407	1.575	62.0	67.8	407	1.560	49.6	65.8
$^{4}G_{11/2}$	377	1.583	1455.3	1466.1	378	1.567	995.8	998.4

Using Sellmeier's dispersion equation, the refractive index could be recalculated at the specific wavelength. Table 2 shows the calculated refractive indices of the samples at the experimentally observed energy level positions of  $\text{Er}^{3+}$ , which were obtained from the absorption spectra as shown in figure 4. Compared with GEr, GErYb and GCErYb have a much stronger absorption band at 980 nm, which results from the  ${}^{2}\text{F}_{7/2} \rightarrow {}^{2}\text{F}_{5/2}$  transition of Yb<sup>3+</sup>. Figure 5 shows



Figure 5. Energy diagram of  $Er^{3+}$  and  $Yb^{3+}$  ions and possible luminescence mechanisms under 980 nm excitation.

the possible sensitizing mechanism and the simplified energy level diagram of  $Er^{3+}/Yb^{3+}$ . When GErYb or GCErYb was excited at 980 nm, the energy transfer from Yb<sup>3+</sup> to  $Er^{3+}$  via the reaction  ${}^{2}F_{5/2}(Yb^{3+}) + {}^{4}I_{15/2}(Er^{3+}) \rightarrow {}^{2}F_{7/2}(Yb^{3+}) + {}^{4}I_{11/2}(Er^{3+})$  would act as indirect pumping of  $Er^{3+}$  and efficiently sensitize the luminescence of  $Er^{3+}$ .

In order to provide a quantitative interpretation of Er<sup>3+</sup> spectral studies in the glass and glass ceramics, the oscillator strengths of all the absorption bands were experimentally measured using expression (1) and parametrically fitted with expression (3). And then the three JO parameters,  $\Omega_t$  (t = 2, 4, 6), were obtained by a least-squares programming technique. Using the three JO parameters, the oscillator strengths of the  $Er^{3+}$  absorption bands could be recalculated in order to evaluate the accuracy of the fit by the root-mean-square (rms) deviation. Table 2 shows the experimental and calculated oscillator strengths, P, of the  $Er^{3+}$  absorption transitions in glass and glass ceramic. Smaller oscillator strengths in GCErYb can be observed in comparison with that in GErYb, which lead to smaller  $\Omega_t$  parameters for GCErYb. The JO parameters  $\Omega_t$  of the Er<sup>3+</sup>/Yb<sup>3+</sup> co-doped glass and glass ceramic, as well as other materials, are given in table 3. In general,  $\Omega_2$  decreases with the increase of symmetry between rare earth ions and the ligand fields and  $\Omega_6$  increases with the decrease of covalency between rare earth ions and the hosts [30–32]. In traditional glasses, the  $\Omega_2$  value decreases with the host changing from oxides to fluorides [33]. From table 3 it can found that the  $\Omega_2$  value of GCErYb was smaller than that of GErYb, which indicates that more  $Er^{3+}$  have entered into the  $CaF_2$ nanocrystal phase in GCErYb. During the crystallization of CaF<sub>2</sub> nanocrystals, Er<sup>3+</sup> ions acted as crystal nuclei. The  $Ca^{2+}$  ions were partially substituted by  $Er^{3+}$  ions. Thus, the  $Er^{3+}$  ions in the CaF2 nanocrystal were mainly coordinated by F<sup>-</sup> ions and a more ionic bond environment of the  $Er^{3+}$  ions can be expected in comparison with that in GErYb. Therefore,  $Er^{3+}$  ions have been incorporated into the CaF2 nanocrystals in GCErYb, which ultimately resulted in the decrease of  $\Omega_2$ . Together with  $\Omega_6$ ,  $\Omega_4$  has an effect on some transitions of  $Er^{3+}$ , such as the  ${}^{4}S_{3/2} \rightarrow {}^{4}I_{15/2}$  transition. The spontaneous transitions of the  ${}^{4}S_{3/2}$  state depend only on the  $\Omega_{4}$ and  $\Omega_6$  parameters due to the reduced matrix elements of the unit tensor  $[U^{(2)}]^2$  that are equal to zero, as shown in table 4. Furthermore, for  ${}^{4}S_{3/2} \rightarrow {}^{4}I_{15/2}$ ,  $[U^{(4)}]^{2}$  is also zero. But  $[U^{(4)}]^{2}$ 

Hosts	$\Omega_2\times 10^{20}~(\text{cm}^2)$	$\Omega_4\times 10^{20}~(\text{cm}^2)$	$\Omega_6\times 10^{20}~(\text{cm}^2)$	$\Omega_4/\Omega_6$
GErYb	5.19	1.59	1.16	1.37
GCErYb	3.37	1.40	1.15	1.22
ZBLAN <sup>a</sup>	2.91	1.27	1.11	1.14
ZBLA <sup>b</sup>	2.54	1.39	0.57	1.43
Fluorophosphate <sup>c</sup>	3.43	1.70	1.29	1.32
Fluorozirconateb	5.6	2.0	1.31	1.52
Phosphatea	6.65	1.52	1.11	1.37
CaF2 <sup>b</sup>	6.6	2.3	2.0	1.15
LaF3 <sup>b</sup>	3.9	1.0	2.3	0.43

**Table 3.** Values of  $\Omega_t$  of the  $Er^{3+}$  ions in the investigated samples and other different glasses.

<sup>a</sup> See reference [33].

<sup>b</sup> See reference [34].

<sup>c</sup> See reference [35].

**Table 4.** The reduced matrix elements of  $Er^{3+}$ .

Transition of Er <sup>3+</sup>	$[U^{(2)}]^2$	$[U^{(4)}]^2$	$[U^{(4)}]^2$
${}^4F_{9/2} \rightarrow  {}^4I_{15/2}$	0.0000	0.5511	0.4621
${}^{4}F_{9/2} \rightarrow {}^{4}I_{13/2}$	0.0109	0.1533	0.0828
${}^{4}F_{9/2} \rightarrow {}^{4}I_{11/2}$	0.0715	0.0101	1.2671
${}^4\mathrm{F}_{9/2} \rightarrow {}^4\mathrm{I}_{9/2}$	0.1220	0.0061	0.0203
$^4S_{3/2} \to  ^4I_{15/2}$	0.0000	0.0000	0.2225
${}^{4}S_{3/2} \rightarrow {}^{4}I_{13/2}$	0.0000	0.0000	0.3419
${}^{4}S_{3/2} \rightarrow {}^{4}I_{11/2}$	0.0000	0.0046	0.0773
${}^4\mathrm{S}_{3/2} \rightarrow {}^4\mathrm{I}_{9/2}$	0.0000	0.0765	0.2569
${}^4S_{3/2} \rightarrow {}^4F_{9/2}$	0.0000	0.0036	0.0014

still has a contribution on the other branching ratio for the  ${}^{4}S_{3/2}$  luminescence. Therefore, small  $\Omega_4$  and large  $\Omega_6$  are necessary for the luminescence corresponding to  ${}^{4}S_{3/2} \rightarrow {}^{4}I_{15/2}$ transition of  $Er^{3+}$ . In order to maximize the luminescence intensity of  ${}^{4}S_{3/2} \rightarrow {}^{4}I_{15/2}$  compared with  ${}^{4}S_{3/2} \rightarrow {}^{4}F_{9/2}$ ,  ${}^{4}S_{3/2} \rightarrow {}^{4}I_{9/2}$ ,  ${}^{4}S_{3/2} \rightarrow {}^{4}I_{11/2}$  and  ${}^{4}S_{3/2} \rightarrow {}^{4}I_{13/2}$  transitions, one requires  $\Omega_4 \ll \Omega_6$ . Thus  $\Omega_4/\Omega_6$  can be used to measure the visible laser corresponding to the  ${}^{4}S_{3/2} \rightarrow {}^{4}I_{15/2}$  transition of  $Er^{3+}$ , which was first introduced by Kaminskii [36] for evaluating the infrared spectroscopic properties of Nd<sup>3+</sup>. The smaller the value of  $\Omega_4/\Omega_6$  is, the more intense the emission intensity of  ${}^{4}S_{3/2} \rightarrow {}^{4}I_{15/2}$  transition is. From table 3 it can be found that the typical range of  $\Omega_4/\Omega_6$  is 0.43–1.52. The smaller  $\Omega_4/\Omega_6$  of GCErYb (1.22) in comparison with that of GErYb (1.37) indicated that GCErYb would exhibit the stronger green luminescence.

Table 5 shows the spontaneous emission probabilities, *A*, branching ratio,  $\beta_{ij}$ , and radiative lifetime,  $\tau$ , of several  $\text{Er}^{3+}$  transitions from state [SL]J to state [S'L']J', which were calculated by using the expressions (9)–(11). Obviously,  $\text{Er}^{3+}$  in GCErYb has a longer radiative lifetime than in GErYb, and at the same time there were no changes of the branching ratios between GErYb and GCErYb. All the above factors, which suggest the probable inclusion of  $\text{Er}^{3+}$  into the CaF<sub>2</sub> nanocrystalline phase, ensure that GCErYb has the more favourable spectroscopic properties, which can be illustrated by the luminescence spectra as shown in figures 6–10.

Figure 6 shows the luminescence spectra (excited at 378 nm with a Xe lamp) of  $Er^{3+}$  in GEr, GErYb and GCErYb. Due to the lower phonon energy of the precipitated  $CaF_2$  nanocystals in GCErYb, a new red emission at 655 nm ( ${}^4F_{9/2} \rightarrow {}^4I_{15/2}$  transition) appeared,

			GErY	b		GCErYb			
[SL]J	[S'L']J'	$A_{\rm ed}~({\rm s}^{-1})$	$A_{\rm md}~({\rm s}^{-1})$	$\beta_{ij}(\%)$	$\tau$ (ms)	$A_{\rm ed}~({\rm s}^{-1})$	$A_{\rm md}~({\rm s}^{-1})$	$\beta_{ij}(\%)$	$\tau$ (ms)
$^{4}I_{13/2}$	${}^{4}I_{15/2}$	79	33	100	8.977	75	32	100	9.328
$^{4}I_{11/2}$	$^{4}I_{15/2}$	96		80	8.327	86		79	9.209
	$^{4}I_{13/2}$	15	9	20		14	9	21	
${}^{4}I_{9/2}$	$^{4}I_{15/2}$	76		70	9.148	65		68	10.404
	$^{4}I_{13/2}$	31		28		29		30	
	${}^{4}I_{11/2}$	1	2	2		1	2	2	
$^{4}F_{9/2}$	$^{4}I_{15/2}$	767		89	1.159	689		89	1.296
	$^{4}I_{13/2}$	46		5		39		5	
	${}^{4}I_{11/2}$	47		5		42		5	
	<sup>4</sup> I <sub>9/2</sub>	3		0		2		0	
${}^{4}S_{3/2}$	$^{4}I_{15/2}$	248		63	2.546	244		63	2.581
	${}^{4}I_{13/2}$	114		29		113		29	
	${}^{4}I_{11/2}$	10		3		10		3	
	<sup>4</sup> I <sub>9/2</sub>	20		5		20		5	
2	<sup>+</sup> F <sub>9/2</sub>	0		0		0		0	
$^{2}H_{11/2}$	<sup>4</sup> I <sub>15/2</sub>	4855		94	0.195	3270		94	0.287
	<sup>4</sup> I <sub>13/2</sub>	96		2		76		2	
	<sup>4</sup> I <sub>11/2</sub>	62 00		1		48		1	
	<sup>4</sup> Eo /2	99 26		2 1		/4 17		2	
	$^{4}S_{3/2}$	0		0		0		0	
4E- 10	4L	1276		73	0 560	1211		74	0.608
<b>F</b> 7/2	<sup>4</sup> I <sub>12</sub> /2	250		14	0.309	217		13	0.008
	$4_{I_{11/2}}$	129		7		117		7	
	<sup>4</sup> I <sub>9/2</sub>	86		5		82		5	
	${}^{4}F_{9/2}$	4	13	1		3	14	1	
	${}^{4}S_{3/2}$	0		0		0		0	
	$^{2}H_{11/2}$	1		0		0		0	
${}^{4}G_{11/2}$	$^{4}I_{15/2}$	17246		85	0.050	11467		84	0.073
,	$^{4}I_{13/2}$	1739		9		1364		10	
	$^{4}I_{11/2}$	80		0		70		1	
	<sup>4</sup> I <sub>9/2</sub>	242		1		163		1	
	${}^{4}F_{9/2}$	750		4		483		4	
	${}^{4}S_{3/2}$	63		0		53		0	
	<sup>2</sup> H <sub>11/2</sub> 4E	23		0		20		0	
	4Eau	42 5		0		29 4		0	
	$^{1}F_{2/2}$	5 7		0		4 6		0	
	$^{2}H_{0/2}$	3	33	0		2		0	

**Table 5.** Spontaneous emission probabilities, A, branching ratio,  $\beta_{ij}$ , and radiative lifetimes,  $\tau$ , of several  $\text{Er}^{3+}$  emission transitions from state [SL1] to state [S'L']!

Properties of  $\rm Er^{3+}/Yb^{3+}$  co-doped  $\rm 50SiO_2-20Al_2O_3-30CaF_2$  glass ceramics

the green emission at 545 nm presented stark split peaks and the blue emission at 408 nm  $(^2H_{9/2} \rightarrow {}^4I_{15/2}$  transition) became more intense in the emission spectra of GCErYb. The ratio of 545 nm  $(^4S_{3/2} \rightarrow {}^4I_{15/2}$  transition) emission intensity to 522 nm  $(^2H_{11/2} \rightarrow {}^4I_{15/2}$  transition) emission intensity significantly increases in GCErYb in comparison with that in GEr and GErYb. It is considered that  ${}^2H_{11/2}$  as well as  ${}^4S_{3/2}$  is populated from upper levels



Figure 6. 378 nm (Xe lamp) excited luminescence spectra of  $Er^{3+}$  doped glass (GEr),  $Er^{3+}/Yb^{3+}$  co-doped glass (GErYb) and glass ceramic (GCErYb).



Figure 7. 980 nm (laser) excited upconversion luminescence spectra of  $Er^{3+}$  doped glass (GEr),  $Er^{3+}/Yb^{3+}$  co-doped glass (GErYb) and glass ceramic (GCErYb).



**Figure 8.** 1064 nm (laser) excited 545 nm luminescence (a) and 655 nm luminescence (b) decay curves of the  $\text{Er}^{3+}/\text{Yb}^{3+}$  co-doped glass (GErYb) and glass ceramic (GCErYb).

by multiphonon relaxation and that these two levels are coupled by a fast thermal equilibrium. The above processes then produces two emissions, centred at 522 and 545 nm, respectively. An analysis based on a simple three-level system comprised of  ${}^{4}I_{15/2}$ ,  ${}^{4}S_{3/2}$  and  ${}^{2}H_{11/2}$  predicts



Figure 9. Dependence of the upconversion luminescence integral intensity of  $Er^{3+}/Yb^{3+}$  co-doped glass ceramic on the LD pumping power.



Figure 10. 980 nm (laser) excited near infrared luminescence spectra of  $Er^{3+}$  doped glass (GEr),  $Er^{3+}/Yb^{3+}$  co-doped glass (GErYb) and glass ceramic (GCErYb).

that thermalization of the  ${}^{2}H_{11/2}$  level can be expressed by the following equation:

$$\frac{I_3}{I_4} = \frac{p_3 g_3 \hbar \omega_3}{p_4 g_4 \hbar \omega_4} \exp\left(\frac{E_{43}}{kT}\right),\tag{15}$$

where the *p* are the total spontaneous emission rates (the reciprocal of the lifetime,  $1/\tau$ ),  $\hbar\omega$  the photon energies, and *g* the degeneracies (2J+1) of the corresponding energy level, respectively. The *I* terms represent the integrated intensity of a given transition at the temperature *T*. The  $E_{43}$  term is the energy gap between the  ${}^{4}S_{3/2}$  and  ${}^{2}H_{11/2}$  levels and *k* is Boltzmann's constant [37]. For GCErYb,  $g_3$ ,  $g_4$ ,  $\hbar\omega_3$ ,  $\hbar\omega_4$  and  $E_{43}$  are almost the same as those of GCErYb, so the value of  $I_3/I_4$  is determined by the value of  $p_3/p_4$  or  $\tau_4/\tau_3$ , and is positively correlated with  $p_3/p_4$  or  $\tau_4/\tau_3$ . The calculated values of  $\tau_4/\tau_3$  from table 5 are 0.077 for GErYb and 0.111 for GCErYb; therefore, lifetime variation led to the inversion of intensity ratio ( ${}^{4}S_{3/2} \rightarrow {}^{4}I_{15/2}$ )/( ${}^{2}H_{11/2} \rightarrow {}^{4}I_{15/2}$ ).

Figure 7 shows the upconversion luminescence spectra (excited at 980 nm) of the  $Er^{3+}/Yb^{3+}$  co-doped glass (GErYb) and the glass ceramic (GCErYb), as well as the  $Er^{3+}$ -doped glass (GEr). It presents a similar character as figure 6. The emission bands can be

**Table 6.** The measured lifetime,  $\tau_{exp}$ , and the luminescence efficiency,  $\eta$ , of the  ${}^{4}S_{3/2}$  and  ${}^{4}F_{9/2}$  levels for  $Er^{3+}$  in GErYb and GCErYb.

	$^{4}S_{2}$	<sub>3/2</sub> (545 nm)		$\frac{{}^{4}\mathrm{F}_{9/2}(655 \text{ nm})}{\tau_{\mathrm{exp}} (\mathrm{ms}) - \tau_{\mathrm{cal}} (\mathrm{ms}) - n (\%)}$		
Sample name	$\tau_{exp}$ (ms)	$\tau_{\rm cal}~({\rm ms})$	$\eta(\%)$	$\tau_{exp}$ (ms)	$\tau_{\rm cal}~({\rm ms})$	η (%)
GErYb GCErYb	0.366 0.390	2.546 2.581	14.38 15.11	0.374 0.505	1.159 1.296	32.27 38.97

assigned to  ${}^{2}H_{9/2} \rightarrow {}^{4}I_{15/2}$  (408 nm),  ${}^{2}H_{11/2} \rightarrow {}^{4}I_{15/2}$  (522 nm),  ${}^{4}S_{3/2} \rightarrow {}^{4}I_{15/2}$  (545 nm) and  ${}^{4}F_{9/2} \rightarrow {}^{4}I_{15/2}$  (655 nm) transitions, respectively. For Er<sup>3+</sup>-doped glass, no upconversion luminescence can be observed. However, intense upconversion luminescence can be observed for Er<sup>3+</sup>/Yb<sup>3+</sup> co-doped glass and glass ceramic. The green and red emissions were so bright that they could be visible to the naked eye when a laser beam of typically 50 mW was used for excitation. This indicates that an effective Yb<sup>3+</sup>  $\rightarrow$  Er<sup>3+</sup> energy transfer upconversion takes place. Furthermore, the upconversion luminescence intensity of GCErYb was much stronger than that of GErYb and the blue upconversion luminescence (408 nm) of GCErYb could also be observed. This can be attributed to the lower phonon energy in the glass ceramic, where Er<sup>3+</sup> and Yb<sup>3+</sup> ions are incorporated into CaF<sub>2</sub> nanocrystals. The clear split emission peaks of GCErYb shown in figure 7 also suggest that some Er<sup>3+</sup> ions are incorporated into CaF<sub>2</sub> nanocrystals. Thus much stronger upconversion luminescence of GCErYb can be obtained.

The above phenomenon can be further confirmed by measuring the luminescence decay curves of  $\text{Er}^{3+}$  that are given in figure 8. These curves are well fitted with first-order exponential decay and can be used to measure the lifetime of excited states. Then the luminescence efficiencies are obtained by using expression (12). Table 6 shows the measured lifetime,  $\tau_{exp}$ , and the luminescence efficiency,  $\eta$ , of the  ${}^{4}S_{3/2}$  and  ${}^{4}F_{9/2}$  levels for  $\text{Er}^{3+}$  in GErYb and GCErYb. The lifetime,  $\tau_{exp}$ , of the  ${}^{4}S_{3/2}$  and  ${}^{4}F_{9/2}$  levels in GCErYb were longer than that in GErYb, which can be attributed to a decreased non-radiative multi-phonon relaxation due to the lower phonon energy around  $\text{Er}^{3+}$  in GCErYb. Therefore, the luminescence efficiencies were improved in GCErYb.

In upconversion processes, the relation between the emission intensity  $I_{em}$  and the IR excitation intensity  $I_{ex}$  is the following:

$$I_{\rm em} \propto \left(I_{\rm ex}\right)^n \tag{16}$$

where *n* is the number of IR photons absorbed per visible photon emitted. Therefore, a plot of  $\log(I_{em})$  versus  $\log(I_{ex})$  should yield a straight line with slope *n*. Figure 9 shows the dependence of the upconversion integral luminescence intensity of GCErYb on the LD pumping power. The slope of  ${}^{2}H_{9/2} \rightarrow {}^{4}I_{15/2}$ ,  ${}^{4}S_{3/2} \rightarrow {}^{4}I_{15/2}$  and  ${}^{4}F_{9/2} \rightarrow {}^{4}I_{15/2}$  emission was 2.45, 1.86 and 1.85, respectively. This result indicated that the  ${}^{4}S_{3/2} \rightarrow {}^{4}I_{15/2}$  and  ${}^{4}F_{9/2} \rightarrow {}^{4}I_{15/2}$  and  ${}^{4}F_{9/2} \rightarrow {}^{4}I_{15/2}$  and  ${}^{4}F_{9/2} \rightarrow {}^{4}I_{15/2}$  transitions were related to a two-photon process and upconversion luminescence corresponding to the  ${}^{2}H_{9/2} \rightarrow {}^{4}I_{15/2}$  transition could be ascribed to three-photon process.

For the green luminescence (at 522 and 545 nm), the possible upconversion luminescence mechanisms of the  $Er^{3+}$  ions can be described by: (1) excited state absorption (ESA), and (2) energy transfer upconversion (ETU) concluding cross relaxation (CR) between two  $Er^{3+}$  ions and energy transfer (ET) between  $Er^{3+}$  ions and  $Yb^{3+}$  ions. In these mechanisms, the 4f-electrons of  $Er^{3+}$  ions at the ground state are excited to the excited state  ${}^{4}I_{11/2}$  by ground state absorption (GSA), CR from adjacent  $Er^{3+}$  ions and ET from  $Yb^{3+}$ . Then they can be excited to the  ${}^{4}F_{7/2}$  level by similar ways of ESA, CR and ET. Finally, the electrons populated rapidly from the  ${}^{4}F_{7/2}$  level to  ${}^{4}S_{3/2}$ ,  ${}^{2}H_{11/2}$  levels by multi-phonon relaxation, which produces two



Figure 11. Absorption cross section and emission cross section of  ${\rm Er}^{3+}/{\rm Yb}^{3+}$  co-doped glass ceramic.

green luminescences, at 522 nm ( ${}^{2}H_{11/2} \rightarrow {}^{4}I_{15/2}$ ) and 545 nm ( ${}^{4}S_{3/2} \rightarrow {}^{4}I_{15/2}$ ). All the above processes have been illustrated in figure 5. ET from Yb<sup>3+</sup> is dominating in the upconversion luminescence of Er<sup>3+</sup>/Yb<sup>3+</sup> co-doped glass and glass ceramic because Yb<sup>3+</sup> has much larger absorption cross section than Er<sup>3+</sup> around 980 nm. The upconversion luminescence of Er<sup>3+</sup> ions is usually baffled by the multiphonon relaxation because there are many metastable energy levels between  ${}^{4}S_{3/2}$ ,  ${}^{2}H_{11/2}$  levels and the ground state. The multiphonon relaxation probability depends primarily upon the energy gap between two successive levels and the phonon energy of the host [38, 39]. The lower the phonon energy of host is, the smaller the multiphonon relaxation probability is. Due to much smaller phonon energy of CaF<sub>2</sub> nanocrystals (~280 cm<sup>-1</sup>) [17] than silicate (~1100 cm<sup>-1</sup>), the upconversion luminescence of Er<sup>3+</sup> ions in the CaF<sub>2</sub> nanocrystals will be stronger than that in the glasses. Thus the upconversion luminescence intensity increased significantly from GErYb to GCErYb.

The electrons on the  ${}^{4}I_{11/2}$  level can also relax to  ${}^{4}I_{13/2}$  by non-radiative multi-phonon relaxation, which will lead to three emissions as shown in figure 5: (1) producing 1530 nm emission by the  ${}^{4}I_{13/2} \rightarrow {}^{4}I_{15/2}$  transition; (2) producing 655 nm emission via the  ${}^{4}I_{11/2} \rightarrow$  ${}^4F_{9/2} \rightarrow {}^4I_{15/2}$  process by absorbing one photon (besides, the  ${}^4S_{3/2} \rightarrow {}^4F_{9/2}$  non-radiative relaxation may also produce 655 nm emission); (3) producing 408 nm emission via the  ${}^{4}I_{11/2} \rightarrow {}^{4}F_{9/2} \rightarrow {}^{2}H_{9/2} \rightarrow {}^{4}I_{15/2}$  process by absorbing other two photons. It is obvious that the  ${}^{4}I_{11/2}$  level plays an important role in all the above upconversion processes. Figure 10 shows the near-infrared luminescence spectra (excited at 980 nm) of the Er<sup>3+</sup> ions in GEr, GErYb and GCErYb. The emission band can be assigned to  ${}^{4}I_{13/2} \rightarrow {}^{4}I_{15/2}$  transition. From the  $Er^{3+}$ doped glass to the  $Er^{3+}/Yb^{3+}$  co-doped glass and glass ceramic, the near-infrared luminescence became significant increased due to the efficient energy transfer from  $Yb^{3+}$  to  $Er^{3+}$ , which ensures their application in 1530 nm optical communication. However, the 1530 nm emission of GCErYb was found to be weaker than that of GErYb. As in the above discussion, the  ${}^{4}I_{11/2}$ level plays an important role in the 980 nm excited upconversion processes. When excited with a 980 nm laser, many more  $Er^{3+}$  4f-electrons at  ${}^{4}I_{11/2}$  in GCErYb were excited to the  $^4F_{7/2}$  state than those in GErYb. Thus the  $Er^{3+}$  4f-electrons at  $^4I_{13/2}$  by relaxation from  $^4I_{11/2}$ were much fewer in GCErYb, which resulted in weaker near-infrared emission of GCErYb in comparison with that of GErYb. For evaluating the stimulated emission properties of  $Er^{3+}$  in GCErYb, figure 11 shows the calculated stimulated emission cross sections and the absorption cross sections of GCErYb that were determined from the absorption spectrum. The emission

Hosts	$\sigma_e \; (\times 10^{-21} \; {\rm cm}^{-1})$	$\tau$ (ms)	FWHM (nm)	$\sigma\times\tau$	FWHM $\times \sigma_e$
GCErYb	5.6	9.3	71	52	398
Fluorosilicatea	7.5	11.0	53	82	398
ZBLAN <sup>a</sup>	5.1	9.5	65	49	331

Table 7. Spectroscopic parameters of the  $^4I_{13/2} \rightarrow {}^4I_{15/2}$  transition for  $Er^{3+}$  in GCErYb, fluorosilicate and ZBLAN hosts.

<sup>a</sup> See reference [41].

cross sections were calculated from the absorption cross sections and the emission spectrum by McCumber theory [40]. The maximum emission cross section is  $5.6 \times 10^{-21}$  cm<sup>-1</sup>, which has been listed in table 7. Er<sup>3+</sup> in GCErYb has very similar emission cross sections and can provide broader bandwidth at about 1530 nm in comparison with ZBLAN and fluorosilicate. Thus the Er<sup>3+</sup>/Yb<sup>3+</sup> co-doped glass ceramic may be a candidate material for near-infrared optoelectronic communication devices.

# 5. Conclusions

 ${\rm Er^{3+}/Yb^{3+}}$  co-doped transparent oxyfluoride glass ceramics containing CaF<sub>2</sub> nanocrystals have been prepared by the heat treatment of the 5 mol% YbF<sub>3</sub> and 0.5 mol% ErF<sub>3</sub> co-doped 50SiO<sub>2</sub>-20Al<sub>2</sub>O<sub>3</sub>-30CaF<sub>2</sub> glasses. Infrared-to-visible upconversion and 1530 nm infrared luminescence in the  ${\rm Er^{3+}/Yb^{3+}}$  co-doped glass and glass ceramics have been observed under 980 nm excitation. The Judd–Ofelt parameters suggested that  ${\rm Er^{3+}}$  ions had been incorporated into CaF<sub>2</sub> nanocrystals in the  ${\rm Er^{3+}/Yb^{3+}}$  co-doped glass ceramics, which resulted in significant increase of the upconversion luminescence intensity of the  ${\rm Er^{3+}/Yb^{3+}}$  codoped glass ceramic in comparison with the  ${\rm Er^{3+}/Yb^{3+}}$  co-doped glass. The red and green upconversion luminescence can be ascribed to a two-photon absorption process and the blue upconversion luminescence to a three-photon absorption process.

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